



任子昌 &lt;rzc1937986979@gmail.com&gt;

## Exploring a Potential Enhancement in SC Decoding of Polar Codes: Seeking Your Insight

3 封邮件

rzc1937986979 &lt;rzc1937986979@gmail.com&gt;

2024年9月23日 23:32

收件人: "arikan@ee.bilkent.edu.tr" &lt;arikan@ee.bilkent.edu.tr&gt;

Dear Professor Erdal Arikan,

I hope this email finds you well.

My name is Zichang Ren, a PhD student from China. I was deeply impressed by your work on polar codes, both for its elegant theoretical foundations and its highly efficient performance, which has greatly inspired my research interest in the field.

I apologize for taking your time, but I have encountered a specific question regarding the Successive Cancellation (SC) decoding algorithm and have been unable to discuss it in depth with anyone around me. I hope to seek your guidance on this matter.

As I understand, the basic idea behind SC decoding is to compute the likelihood of  $U_i$  given  $U_1, U_2, \dots, U_{i-1}$ , and this process is carried out sequentially from  $i=1$  to  $i=N$ . However, I noticed that the algorithm does not seem to utilize the known frozen bits after  $U_i$ , i.e.,  $U_{i+1}, U_{i+2}, \dots, U_N$ . This made me wonder if incorporating this information could potentially improve the decoding performance.

After implementing this idea in code, I regrettably found that it did not result in a lower error rate. In fact, it seems that the following equality holds:

$$H(U_i | U_{i-1}) = H(U_i | U_{i-1}, U_A)$$

where  $A$  is the set of frozen bit indices.

I've been pondering this issue for a while without any clear insight. I would greatly appreciate it if you could share your thoughts on this matter. Your response would mean a lot to me.

Thank you very much for your time and consideration.

Best regards,  
Zichang Ren

Erdal Arikan &lt;arikan@ee.bilkent.edu.tr&gt;

2024年9月24日 16:43

收件人: rzc1937986979 &lt;rzc1937986979@gmail.com&gt;

Dear Zichang,

If we let  $U^i = U_1, \dots, U_i$ , the equality  $H(U_i | U^{i-1}) = H(U_i | U^{i-1}, U_A)$  is not exact but should hold asymptotically due to polarization. I guess with the insight you have, you should be able to prove the asymptotic result. You should give it a try.

Best,

Erdal

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rzc1937986979 &lt;rzc1937986979@gmail.com&gt;

2024年9月25日 14:09

收件人: Erdal Arikan &lt;arikan@ee.bilkent.edu.tr&gt;

Dear Professor Arıkan,

Thank you very much for your response and guidance. I will definitely try to prove the asymptotic result as suggested.

Best regards,  
Zichang Ren